

# Motion in molecules and Spectra



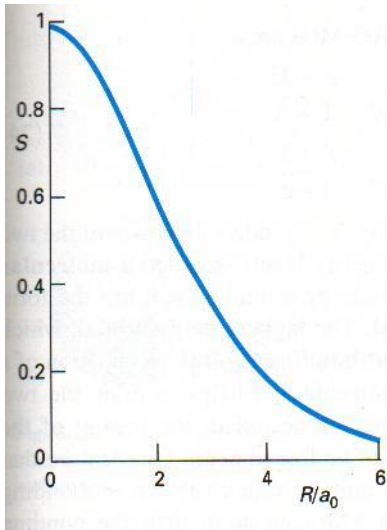
Gerhard Herzberg,  
Nobel 1971

"for his contributions to the knowledge  
of electronic structure and geometry  
of molecules,  
particularly free radicals"

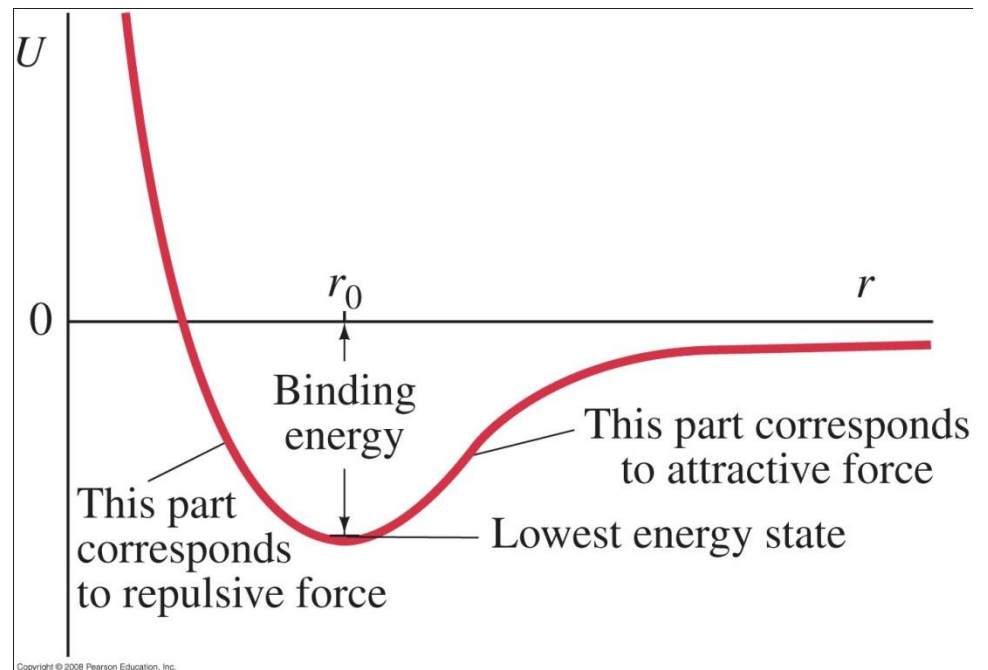
# Potential-Energy Diagrams for Molecules

For the hydrogen molecule, the force between the atoms is attractive at large distances. There is a minimum in the potential.

Overlap integral is a function of  $R$

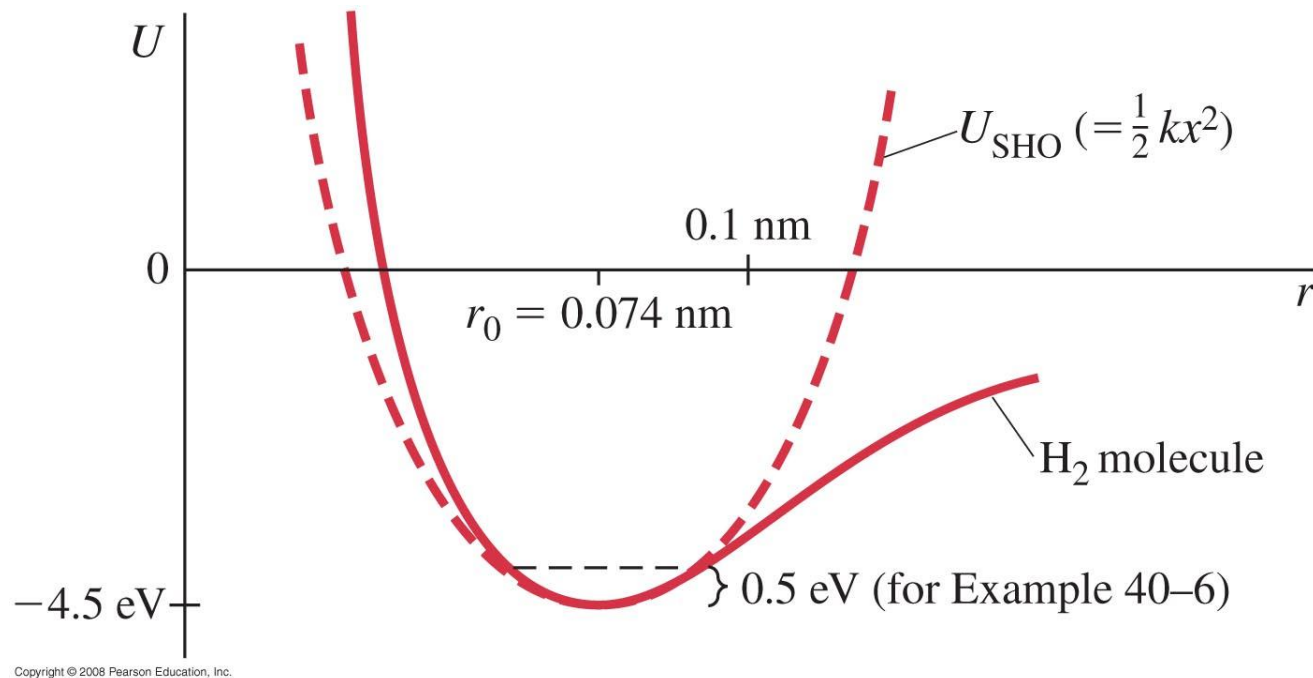


Also account for  
repulsion of nuclei



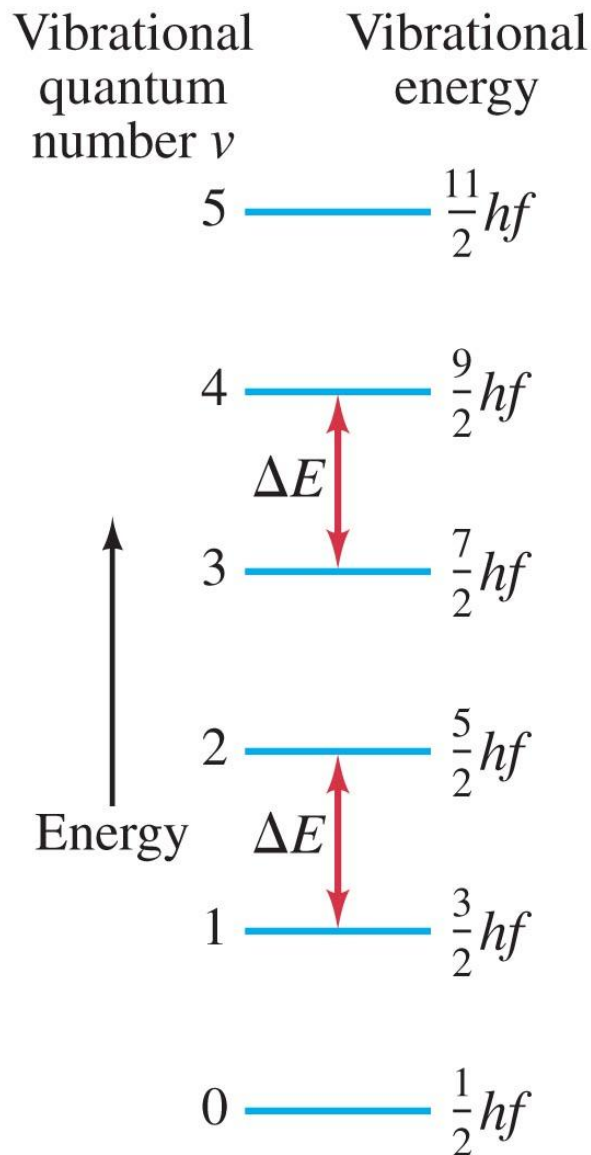
# Molecular Spectra

Small-amplitude vibrations of a diatomic molecule will be simple harmonic. Again, the energy is quantized.



Treat this potential with the Schrödinger Equation  
Think about the meaning of the wave function !!

# Molecular Spectra



Here are some vibrational energy levels in a diatomic molecule, and the allowed transitions.

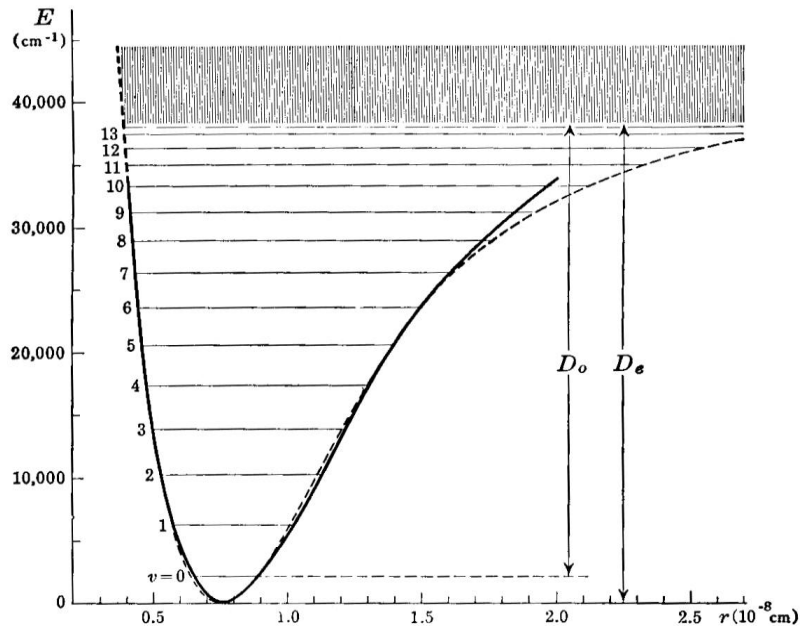
Quantum jumps between levels of vibrational energy give rise to an additional spectrum:

**vibrational spectroscopy**

→ **Infrared spectra**

(Study the magnitude of frequency separations in vibrations)

# Potential energy curve of a real molecule: H<sub>2</sub>



**H<sub>2</sub> has 14 bound vibrational energy levels.**  
**D<sub>2</sub> has 17.**

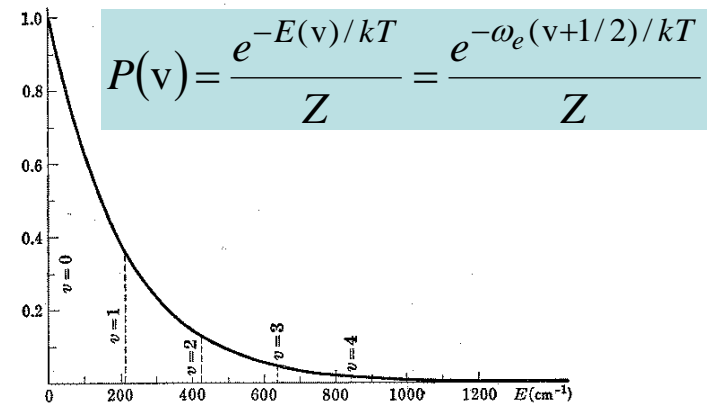


FIG. 58. Boltzmann Factor and Thermal Distribution of the Vibrational Levels. The curve gives the function  $e^{-E/kT}$  for  $T = 300^\circ \text{ K}$ . with  $E$  in  $\text{cm}^{-1}$ . The broken-line ordinates correspond to the vibrational levels of the I<sub>2</sub> molecule.

RATIO OF THE NUMBER OF MOLECULES IN THE FIRST TO THAT IN THE ZEROth VIBRATIONAL LEVEL FOR  $300^\circ \text{ K}$ . AND  $1000^\circ \text{ K}$ .

Gas	$\Delta G_{1/2}(\text{cm}^{-1})$	$e^{-\Delta G_{1/2}hc/kT}$	
		For $300^\circ \text{ K}$ .	For $1000^\circ \text{ K}$ .
H <sub>2</sub>	4160.2	$2.16 \times 10^{-9}$	$2.51 \times 10^{-3}$
HCl	2885.9	$9.77 \times 10^{-7}$	$1.57 \times 10^{-2}$
N <sub>2</sub>	2330.7	$1.40 \times 10^{-5}$	$3.50 \times 10^{-2}$
CO	2143.2	$3.43 \times 10^{-5}$	$4.58 \times 10^{-2}$
O <sub>2</sub>	1556.4	$5.74 \times 10^{-4}$	$1.07 \times 10^{-1}$
S <sub>2</sub>	721.6	$3.14 \times 10^{-2}$	$3.54 \times 10^{-1}$
Cl <sub>2</sub>	556.9	$6.92 \times 10^{-2}$	$4.49 \times 10^{-1}$
I <sub>2</sub>	213.2	$3.60 \times 10^{-1}$	$7.36 \times 10^{-1}$

# Molecular Spectra

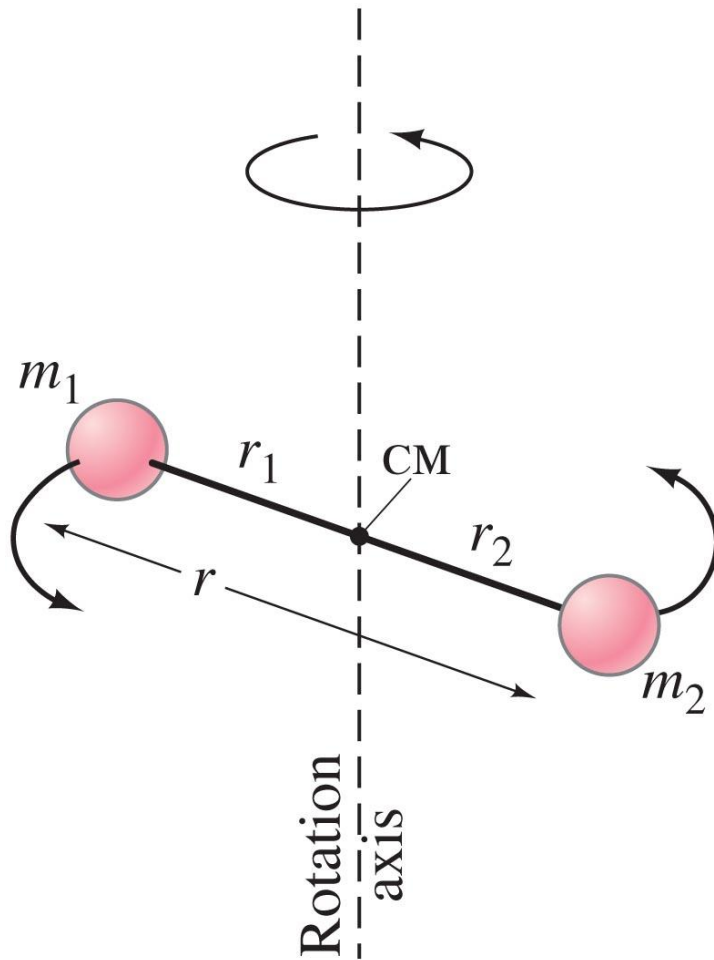
A diatomic molecule can rotate around a vertical axis. The rotational energy is quantized.

## Reduced mass.

moment of inertia of a diatomic molecule rotating about its center of mass can be written

$$I = \mu r^2,$$

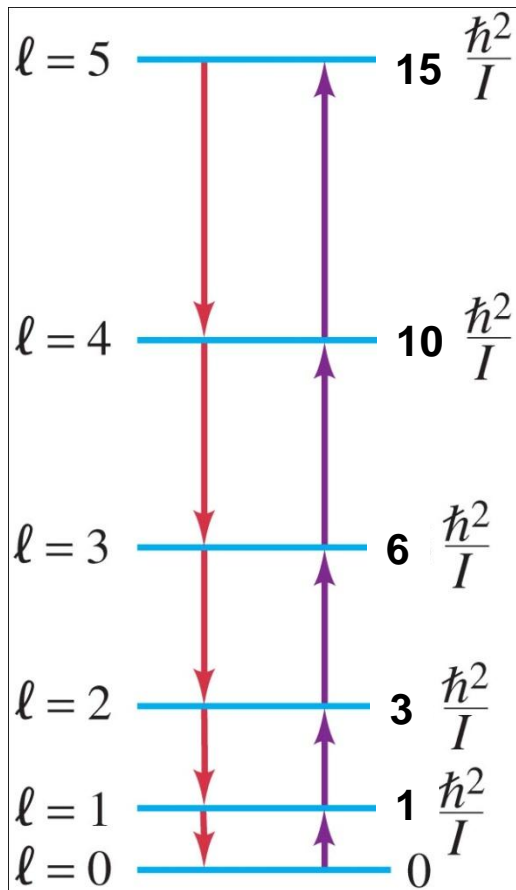
$$\mu = \frac{m_1 m_2}{m_1 + m_2}$$



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Angular momentum  $L = I\omega$

# Molecular Spectra (purely rotational)



These are some rotational energy levels and allowed transitions for a diatomic molecule.

$$E = \frac{1}{2} I \omega^2 = \frac{L^2}{2I}$$

Rotation in a molecule related to angular momentum; Quantization analogous to electron in atom

$$E = \frac{\hbar^2}{2I} \ell(\ell + 1)$$

Rotational quantum number mostly given as  $J$

Determination of the equilibrium separation  $R_e$  from the spectrum

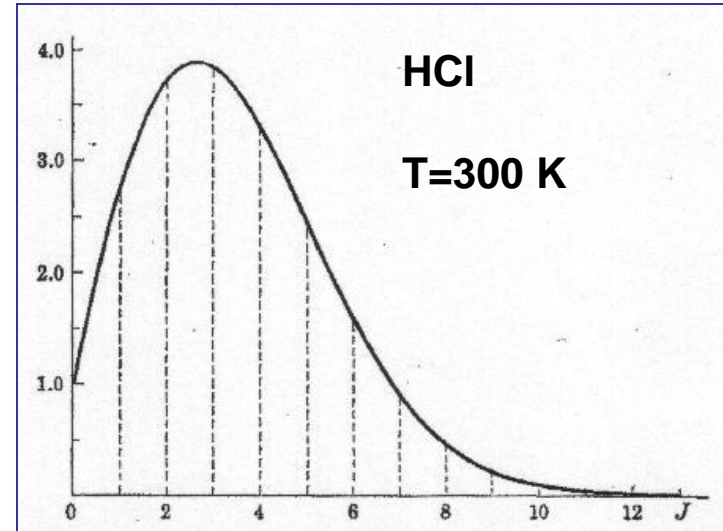
# Population distributions rotational states in a diatomic molecule

Probability of finding a molecule  
in a rotational quantum state:

$$P(J) = \frac{(2J+1)e^{-E_{rot}/kT}}{\sum_{J'} (2J'+1)e^{-E_{rot}/kT}}$$
$$= \frac{1}{Z_{rot}} (2J+1)e^{-BJ(J+1)+DJ^2(J+1)^2}$$

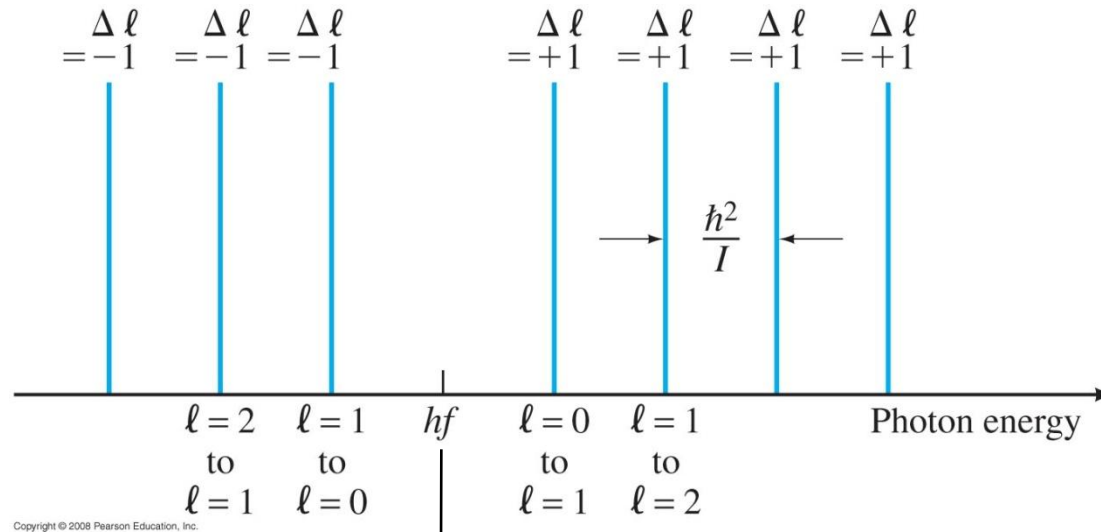
Find optimum via

$$\frac{dP(J)}{dJ} = 0$$

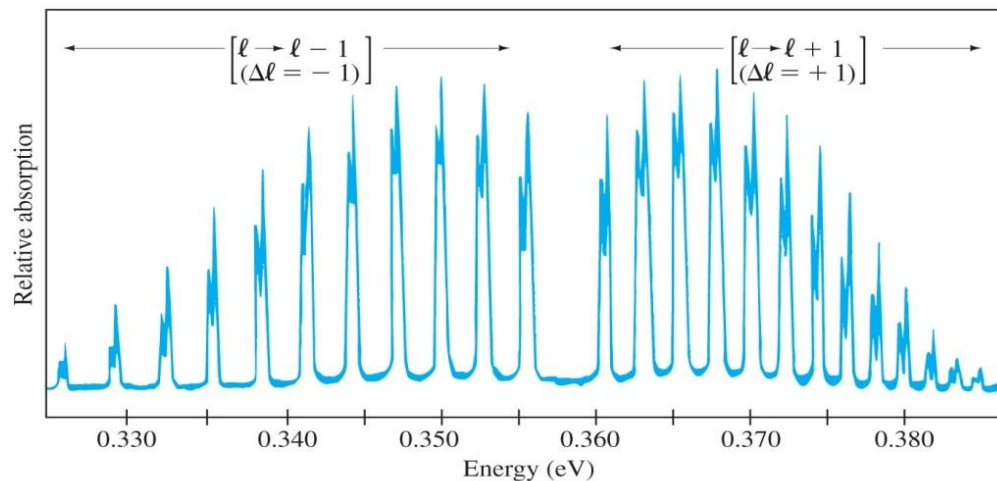




# Vibrational Spectra (ro-vibrational)



Location of “vibrational band origin”



Spacing between lines is

$$\Delta E = \frac{\hbar^2}{I}$$

$$R_e = \sqrt{\frac{I}{\mu}}$$

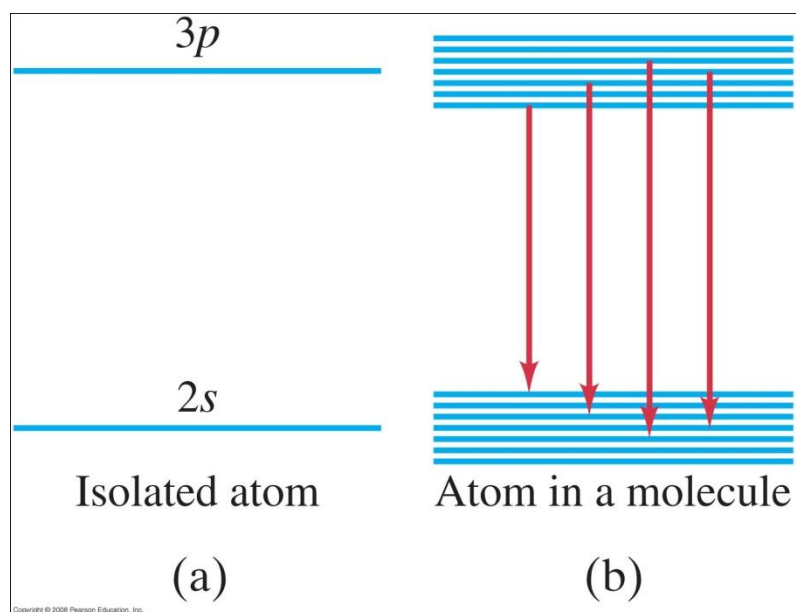
$$\mu = \frac{M_H M_{Cl}}{M_H + M_{Cl}}$$

↘  
**Bond length**

# Molecular Spectra

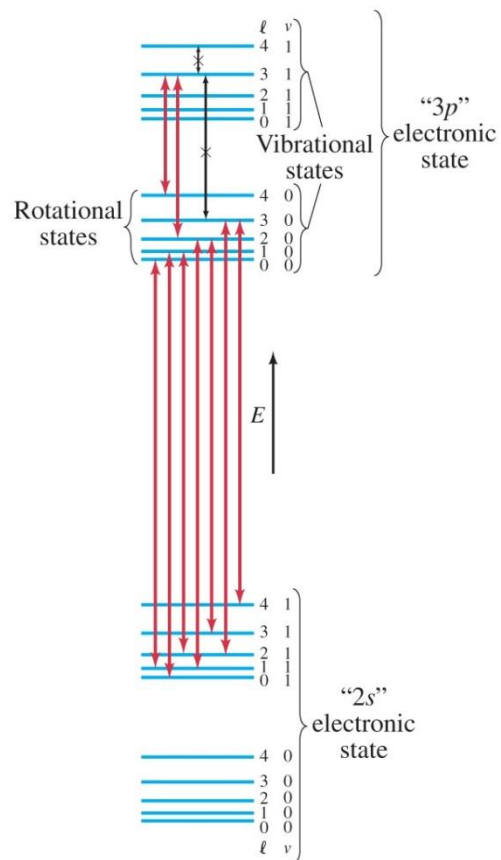
The overlap of orbits alters energy levels in molecules. Also, more types of energy levels are possible, due to rotations and vibrations. The result is a **band** of closely spaced energy levels:

**Molecular band spectra** (electronic transitions, with vibration and rotation superimposed); → Selection rules



# Molecular Spectra

electronic transitions, with vibration and rotation superimposed)



→ Selection rules

Franck-Condon principle

P, Q, R transitions