

**Sheinman, Sharma, and MacKintosh Reply:** The authors of the preceding Comment [1] raise an interesting question about ambiguities in defining the Fisher exponent  $\tau$ . Ordinarily, such critical exponents are determined by the behavior in the thermodynamic limit. In the percolation theory context the number of connected clusters with mass  $s$  scales as [2,3]

$$n_s \propto s^{-\tau} \quad (1)$$

in the infinite size limit,  $M \rightarrow \infty$ , up to possible logarithmic corrections. To estimate the value of  $\tau$  numerically, however, one must consider systems with finite  $M$ , together with an appropriate finite-size scaling consistent with Eq. (1) as  $M \rightarrow \infty$ . As in the Comment [1], one approach often used in the percolation literature [3] is

$$n_s = Ms^{-\tau} f\left(\frac{s}{M^{d_f/d}}\right), \quad (2)$$

where  $d$  is the dimensionality ( $d = 2$  here) and  $d_f$  is the fractal dimension of the clusters. The function  $f(s/M^{d_f/d})$  is constrained to have no power-law dependence in the regime  $1 \ll s \ll M$  and has to vanish for  $s > M$ . In random percolation (RP)  $d_f < 2$  and  $\tau = d/d_f + 1 > 2$  [3]. Demanding conservation,

$$\int_1^\infty sn_s ds = M, \quad (3)$$

means that Eq. (2) is consistent with (1) only for  $\tau \geq 2$ . Thus, the approach in the Comment [1] presupposes that

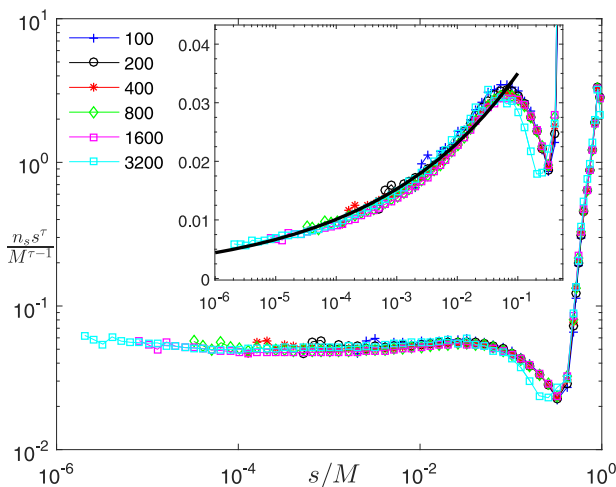


FIG. 1. Collapse attempts of the cluster masses distribution of the NEP model [4] at  $p = p_c$  using  $\tau = 1.82 < 2$  (main figure) with definition (4) and  $\tau = 2$  with equivalent (for this value of  $\tau$ ) definitions (2) and (4) (inset) for different system sizes (see the values of  $\sqrt{M}$  in the legend). The line in the inset corresponds to the power law with  $0.18 = 2 - 1.82$  exponent.

$\tau \geq 2$  and is incapable of identifying possible values of  $\tau < 2$ .

For this reason, in addition to the standard RP ansatz, we also used an ansatz consistent with Eq. (1), while allowing for possible  $\tau < 2$ :

$$n_s = M^{\tau-1} s^{-\tau} f\left(\frac{s}{M}\right). \quad (4)$$

This is consistent with Eq. (1), while satisfying Eq. (3) for  $\tau < 2$ . In general, with no information about  $\tau$  being larger or smaller than 2, one should analyze the numerical data for both cases. We do this in Fig. 1, e.g., by plotting  $s^\tau n_s / M^{\tau-1}$  vs  $s/M$  for the case  $\tau < 2$ . We find good collapse and near constancy of  $s^\tau n_s / M^{\tau-1}$  for  $\tau = 1.82$  and over a wide range of  $s/M$  up to  $\sim 0.1$ . By contrast, attempting the same collapse for  $\tau = 2$ , where both our ansatz and that of the Comment [1] are equivalent, we do not find the expected near constancy of  $s^2 n_s / M$ . Thus, while it may not be possible to entirely rule out  $\tau = 2$  with significant logarithmic corrections, our results appear to be more consistent with  $\tau = 1.82$ . In the inset, however, we have plotted the distribution log-linear, in a way closely analogous to the Comment [1]. Here, we do not find evidence of a logarithmic dependence. Our data are, in fact, consistent with a weak exponent 0.18, as indicated by the thick line.

We thank the authors of the Comment [1] for their interest and the useful discussion of subtleties in interpreting the numerical data. But, we fundamentally disagree with their approach that tacitly assumes  $\tau \geq 2$ .

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